

FULL PORTION TEST SERIES 2019 – 2020.**MATHS****SECTION I (40)****[ANSWERS]**

1.

$$\begin{aligned}
 \text{a. } S_n &= \frac{n}{2} [2a + (n-1)d] \\
 0 &= \frac{15}{2} [2a + (14)d] \\
 0 &= 2a + 14d \\
 0 &= a + 7d \\
 a + 3d &= 12 \\
 -a + 7d &= 0 \\
 \hline
 -4d &= 12 \\
 d &= -3 \\
 a + 7d &= 0 \\
 a - 21 &= 0 \\
 a &= \underline{\underline{21}} \\
 t_{12} &= a + 11d \\
 &= 21 + 11(-3) \\
 &= 21 - 33 \\
 &= \underline{\underline{-12}}
 \end{aligned}$$

b.

i. 2×1

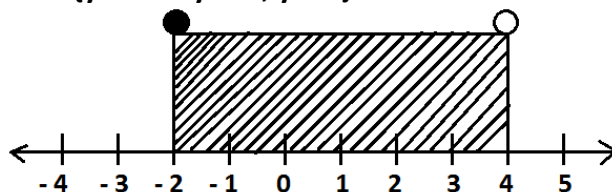
$$\begin{aligned}
 \text{ii. Let } X &= \begin{bmatrix} x \\ y \end{bmatrix} \\
 \begin{bmatrix} 6 & -2 \\ 2 & 3 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} &= \begin{bmatrix} 10 \\ -4 \end{bmatrix} \\
 \begin{bmatrix} (6 \times x) + (-2 \times y) \\ (2 \times x) + (3 \times y) \end{bmatrix} &= \begin{bmatrix} 10 \\ -4 \end{bmatrix} \\
 \begin{bmatrix} 6x - 2y \\ 2x + 3y \end{bmatrix} &= \begin{bmatrix} 10 \\ -4 \end{bmatrix} \\
 6x - 2y &= 10 \\
 (3x - y) &= 5 \quad \times 3 \\
 9x - 3y &= 15 \quad \dots (i) \\
 2x - 3y &= -4 \quad \dots (ii)
 \end{aligned}$$

Adding equation (i) and (ii)

$$\begin{array}{rcl}
 9x - 3y & = & 15 \\
 + 2x + 3y & = & -4 \\
 \hline
 11x & = & 11 \\
 x & = & 1 \\
 3x - y & = & 5 \\
 3 - y & = & 5
 \end{array}$$

$$\begin{array}{rcl}
 y & & = 3 - 5 \\
 y & & = -2 \\
 x & & = \begin{bmatrix} 1 \\ -2 \end{bmatrix}
 \end{array}$$

c. $2y - 3 < y + 1 \leq 4y + 7; y \in \mathbb{R}$
 $2y - 3 < y + 1; y + 1 \leq 4y + 7$
 $-3 - 1 < y - 2y; y - 4y \leq 7 - 1$
 $-4 < -y; -3y \leq 6$
 $4 > y; y \geq -2$
 $-2 \leq y < 4$
 $S.S = \{y: -2 \leq y < 4; y \in \mathbb{R}\}$



2.

a. $n(s)$ $= 31$
 No. of days in week $= 7$
 If first of January is Monday $= 1, 8, 15, 22, 29$
 If second of January is Monday $= 2, 9, 16, 23, 30$
 If third of January is Monday $= 3, 10, 17, 24, 31$
 So no. weeks with 5 Mondays $= 3 \text{ } n(A)$
 i. Probability (leap year)
 $= \frac{\text{no. of favourable outcomes}}{\text{total no. of outcomes}}$
 $= \frac{n(A)}{n(S)}$
 $= \frac{3}{7}$

ii. For a non-leap year, the probability will be the same because January has the same number of days. $= \frac{3}{7}$

b. $(k+2)x^2 - kx + 6 = 0$
 $(k+2)(3)^2 - (k)(3) + 6 = 0$
 $(k+2)(9) - 3k + 6 = 0$
 $9k + 18 - 3k + 6 = 0$
 $6k + 24 = 0$
 $6k = -24$
 $k = -4$
 $(k+2)x^2 - kx + 6 = 0$
 $(-4+2)x^2 - (-4)x + 6 = 0$
 $-2x^2 + 4x + 6 = 0$
 $a = -2$
 $b = 4$
 $c = 6$
 $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
 $= \frac{-(4) \pm \sqrt{(4)^2 - 4(-2)(6)}}{2(-2)}$
 $= \frac{-4 \pm \sqrt{16 + 48}}{-4}$

$$\begin{aligned}
 &= \frac{-4 \pm 8}{-4} \\
 &= \frac{+4(-1 \pm 2)}{-4} \\
 &= \frac{-1 \pm 2}{-1} \\
 &= \frac{-1-2}{-1} \\
 x &= \frac{-1+2}{-1} \quad \text{Or } x = \frac{-1-2}{-1} \\
 &= \frac{1}{-1} \quad \text{Or } = \frac{-3}{-1} \\
 &= -1 \quad \text{Or } = 3 \\
 x &= \{-1, 3\}
 \end{aligned}$$

C.

C.I.	Continuous C.I.	x	f	d	t	Ft
0 – 9	– 0.5 – 9.5	4.5	4	– 40	– 4	– 16
10 – 19	9.5 – 19.5	14.5	6	– 30	– 3	– 18
20 – 29	19.5 – 29.5	24.5	12	– 20	– 2	– 24
30 – 39	29.5 – 39.5	34.5	6	– 10	– 1	– 6
40 – 49	39.5 – 49.5	44.5	7	0	0	0
50 – 59	49.5 – 59.5	54.5	5	+ 10	1	5
60 – 69	59.5 – 69.5	64.5	2	+ 20	2	4
70 – 79	69.5 – 79.5	74.5	8	+ 30	3	24

$$\sum f = 50$$

$$\sum f = -64 + 33$$

$$= -31$$

$$\bar{x} = A + \frac{\sum ft}{\sum f} \times i$$

$$= 44.5 + \frac{-31}{50} \times 10$$

$$= 44.5 - 6.2$$

$$= \underline{\underline{38.3}}$$

3.

$$\begin{aligned}
 \text{a. } \frac{a^3 + 3ab^2}{3a^2b + b^3} &= \frac{x^3 + 3xy^2}{3x^2y + y^3} \\
 \frac{a^3 + 3ab^2 + 3a^2b + b^3}{a^3 + 3ab^2 - 3a^2b - b^3} &= \frac{x^3 + 3xy^2 + 3xy^2 + y^3}{x^3 + 3xy^2 - 3x^2y - y^3} \\
 \frac{(a+b)^3}{(a-b)^3} &= \frac{(x+y)^3}{(x-y)^3}
 \end{aligned}$$

Taking cube root on both sides

$$\frac{a+b}{a-b} = \frac{x+y}{x-y} \quad (\text{By C and D})$$

$$\frac{a+b+a-b}{a+b-a+b} = \frac{x+y+x-y}{x+y-x+y}$$

$$\frac{2a}{2b} = \frac{2x}{2y}$$

$$\frac{a}{b} = \frac{x}{y} \quad (\text{By alternate})$$

$$\frac{y}{b} = \frac{x}{a}$$

Hence proved

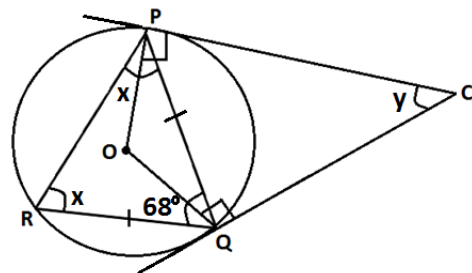
- b. n = 3 years
 = 36 months
 r = 8%
 I = Rs. 1776
 P = ?
 MV = ?

$$\begin{aligned}
 I &= \frac{P \times n(n+1) \times r}{2 \times 12 \times 100} \\
 1776 &= \frac{P \times 36 \times 37 \times 8}{2 \times 12 \times 100} \\
 16 \times 25 &= P \\
 \therefore P &= \text{Rs. } 400 \\
 MV &= P \times n + I \\
 MV &= 400 \times 36 + 1776 \\
 MV &= 14400 + 1776 \\
 MV &= \text{Rs. } 16176
 \end{aligned}$$

c. $f(x) = x^3 + 2x^2 - 5ax - 7$
 let $(x+1)$ $= 0$
 $x = -1$
 $f(x) = R$, By R. theorem
 $f(x) = x^3 + 2x^2 - 5ax - 7$
 $= (-1)^3 + 2(-1)^2 - 5(a)(-1) - 7$
 $= -1 + 2(1) + 5a - 7$
 $= -1 + 2 + 5a - 7$
 $P = 5a - 6$
 $f(x) = x^3 + ax^2 - 12x + 6$
 $x - 2 = 0$
 $x = 2$
 $f(x) = R$; By R. theorem
 $= (2)^3 + a(2)^2 - 12(2) + 6$
 $= 8 + a(4) - 24 + 6$
 $= 8 + 4a - 18$
 $Q = 4a - 10$
 $2P + Q = 6$
 $2(5a - 6) + (4a - 10) = 6$
 $10a - 12 + 4a - 10 = 6$
 $14a - 22 = 6$
 $14a = 28$
 $a = \underline{2}$

4.

- a. Given:
 i. $PQ = RQ$
 ii. $\angle RQP = 68^\circ$
 To find:
 i. x
 ii. y



	Statement	Reason
1.	In $\triangle RPQ$,	
i.	$PQ = RQ$	Given
ii.	$\angle QRP = \angle QPR = a$	Angles opposite equal sides are equal
iii.	In $\triangle RPQ$,	
	$\angle QRP + \angle QPR + \angle RQP = 180^\circ$	Sum of the angles of triangle is 180°
	$a + a + 68^\circ = 180^\circ$	
	$2a = 112^\circ$	
	$a = 56^\circ$	

2.	$\angle QOP$	$= 2 \angle QRP$ $= 2 \times 56^\circ$ $= 112^\circ$	Angles in the same segment
3.	In $\triangle POQ$,		
i.	PO	$= QO$	Radii of same circle angles opposite equal sides are equal.
ii.	$\angle OQP = \angle OPQ$	$= b$	
iii.	$b + b + 112^\circ$	$= 180^\circ$	
	$2b$	$= 68$	
	b	$= 32^\circ$	Tangent perpendicular to radius at point of contact. By addition property
4.	$\angle QPC = \angle OQC$	$= 90^\circ$	
5.	$\angle QPC$	$= \angle OPC - \angle OPQ$ $= 90^\circ - 32^\circ$ $= 48^\circ$	
	$\angle QPC = \angle PQC$	$= 48^\circ$	Sum of all angles of triangle is 180° .
	$48^\circ + 48^\circ + y$	$= 180^\circ$	
	y	$= 84^\circ$	

b. A to B:

Meerut (UP) to Ratlam (MP) – Inter-state: IGST

$$\begin{aligned}
 \text{Selling price} &= 15,000 \\
 \text{IGST 18\%} &= \frac{18}{100} \times 15,000 \\
 &= 2,700 \\
 \text{Amount of bill} &= 15,000 + 2,700 \\
 &= \text{Rs. } 17,700
 \end{aligned}$$

B to C:

Ratlam (MP) to Jabalpur (MP) – Inter-state: (CGST and SGST)

$$\begin{aligned}
 \text{Cost price} &= 15,000 \\
 \text{Profit} &= 3,000 \\
 \text{Selling price} &= 18,000 \\
 \text{CGST 9\%} &= \frac{9}{100} \times 18,000 \\
 &= 1,620 \\
 \text{SGST 9\%} &= \frac{9}{100} \times 18,000 \\
 &= 1,620 \\
 \text{Total tax} &= 3,240 \\
 \text{Net tax} &= 3,240 - 2,700 \\
 &= \underline{540} \\
 \text{Amount of bill} &= 18,000 + 3,240 \\
 &= \text{Rs. } \underline{\underline{21,240}}
 \end{aligned}$$

$$\begin{aligned}
 \text{c. } \frac{24}{18-x} - \frac{24}{18+x} &= 1 \\
 24 \left(\frac{1}{18-x} - \frac{1}{18+x} \right) &= 1
 \end{aligned}$$

$$24 \left(\frac{(18+x) - (18-x)}{(18-x)(18+x)} \right) = 1$$

$$24 \left(\frac{18+x-18+x}{324-x^2} \right) = 1$$

$$24 \left(\frac{2x}{324-x^2} \right) = 1$$

$$484 = 324 - x^2$$

$$x^2 + 484 - 324 = 0$$

$$x^2 + 54x - 64 - 324 = 0$$

$$(x+54)(x-6) = 0$$

$$x = 6 \quad x = -54$$

Ignoring negative

$\therefore \underline{x=6}$ km/hr.

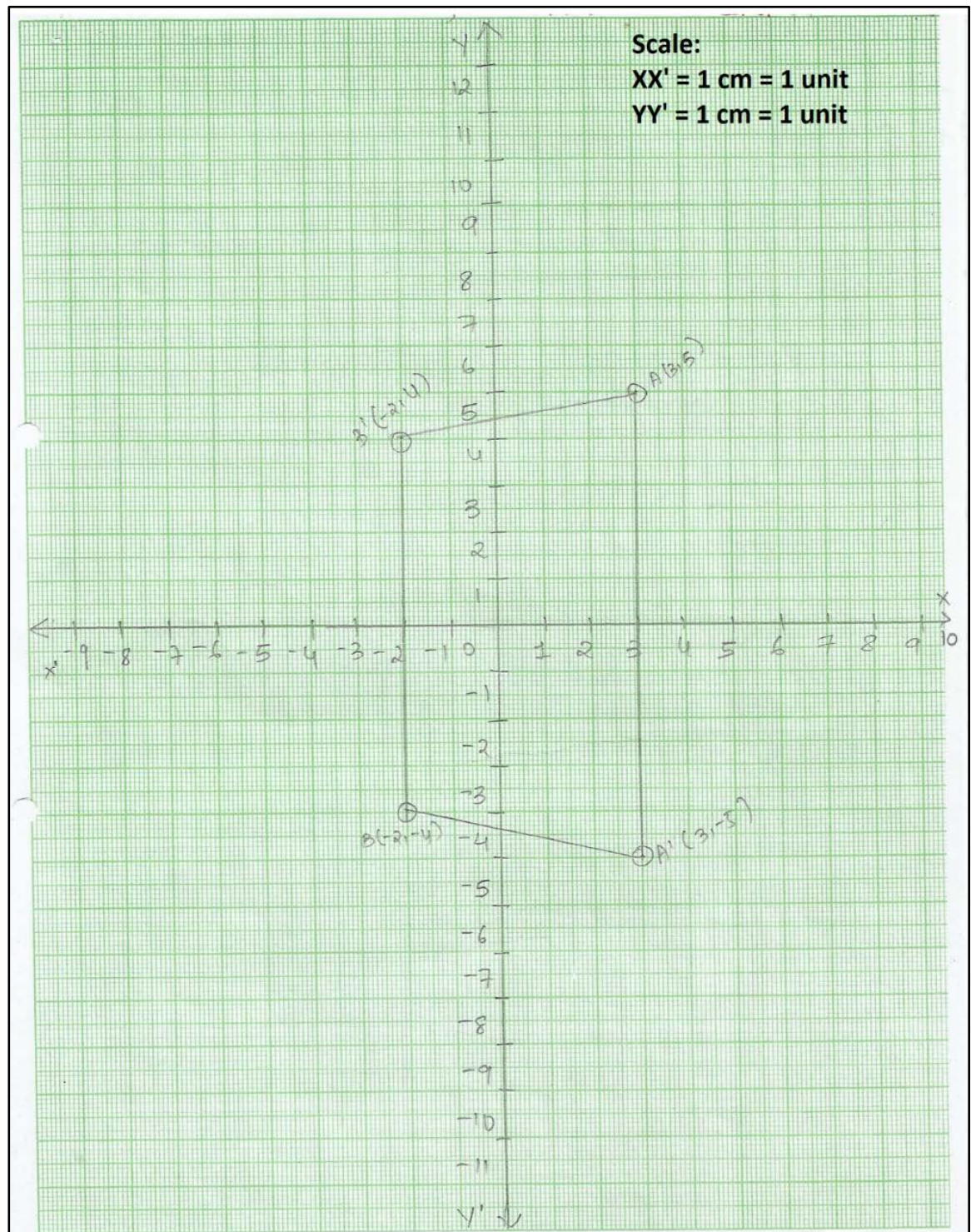
d.

i. $A' (3, -5)$

ii. $B' (-2, 4)$

iii. Trapezium

iv. $(-2, 0), (3, 0)$



5.

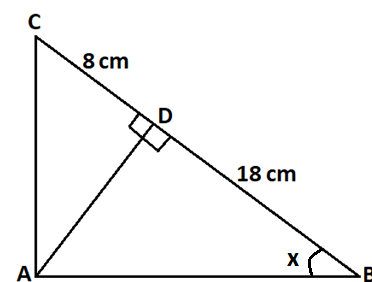
a. **Given:**

- i. $\angle BAC = \angle BDA = \angle CDA = 90^\circ$
- ii. $CD = 8 \text{ cm}$
- iii. $BD = 18 \text{ cm}$

To find:

- i. AD
- ii. $\frac{A(\triangle ADB)}{A(\triangle CDA)}$

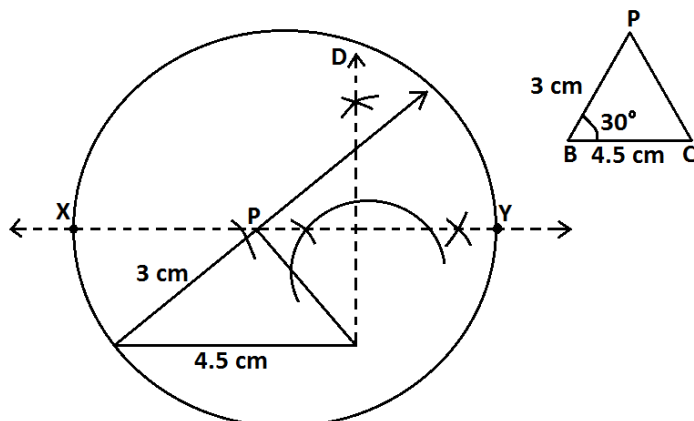
TPT: $\triangle ADB \sim \triangle CDA$



	Statement	Reason
1.	Let $\angle CBA = x$	
2.	In $\triangle CBA$,	
i	$\angle ACB = 180 - (90 + x)$ $= (90 - x)^\circ$	Sum of angles of triangle is 180°
3.	In $\triangle ADB$,	
i	$\angle DAB = 180 - (90 + x)$ $= (90 - x)^\circ$	Sum of angles of triangle is 180°
4.	In $\triangle ADB$ and $\triangle CDA$	
i	$\angle ADB = \angle CDA = 90^\circ$	Given
ii	$\angle DCA = \angle DAB$	From 2(i) and 3 (i)
iii	$\triangle ADB \sim \triangle CDA$	By AA postulate
5.	$\frac{AD}{CD} = \frac{AB}{CA} = \frac{DB}{DA}$ $AD^2 = CD \times DB$ $AD = \sqrt{18 \times 8}$ $AD = \sqrt{144}$ $AD = \underline{12\text{cm}}$	Corresponding sides of similar triangle are in proportional
6.	$\frac{A(\triangle ADB)}{A(\triangle CDA)} = \frac{AD^2}{CD^2}$ $= \frac{12 \times 12}{8 \times 8}$ $= \frac{9}{4}$ $A(\triangle ADB): A(\triangle CDA) = \underline{9:4}$	When two triangle are similar, ratio of their angle is equal to ratio of the square on their corresponding sides.

b. a = 45
d = 41 - 45
= -4
first negative term = -3
 $\therefore t_n = -3$
 $a + (n - 1) d = -3$
 $45 + (n - 1) (-4) = -3$
 $-4n + 4 = -3 - 45$
 $-4n + 4 = -3 - 45$
 $-4n = -48 - 4$
 $-4n = -52$
n = 13

c.



6.

a.

$m_1 = 3$ A $(x, 0)$	$m_2 = 1$ P $(3, 2)$	B $(0, y)$
$\alpha = \frac{m_1 x_2 + m_2 x_1}{m_1 + m_2}$;	$\beta = \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2}$	
$3 = \frac{3(0) + 1(x)}{3 + 1}$;	$2 = \frac{3(y) + 1(0)}{3 + 1}$	
$3 = \frac{0 + x}{4}$;	$2 = \frac{3y + 0}{4}$	
$x = 12$;	$\frac{8}{3} = y$	
A (x, 0) = (12, 0)	B (0, y) = (0, $\frac{8}{3}$)	

b. F.V. = Rs. 26

n = ?

r = 10%

MV = Rs. 28

I = Rs. 20020

D = ?

R = ?

i. $I = MV \times n$

$20020 = 28 \times n$

$n = \frac{20020}{28}$

$= \underline{\underline{715 \text{ shares}}}$

ii. $D = \frac{FV \times n \times r}{100}$

$= \frac{26 \times 715 \times 10}{100}$

$= \underline{\underline{\text{Rs. 1895}}}$

iii. $FV \times r = MV \times R$

$26 \times 10 = 28 \times R$

$\frac{26 \times 10}{28} = R$

$R = \frac{65}{7}$

$R = 9\frac{2}{7} \%$

c.

i. $K = 1:4500$

ii. Height of model = 90cm
 $k = \frac{\text{height of model}}{\text{actual height}}$

$\frac{1}{4500} = \frac{90}{\text{actual height}}$

Actual height = 90×4500

$= 405000 \text{ cm}$

$= \underline{\underline{4050 \text{ m}}}$

iii. $K^3 = \frac{\text{vol. of model}}{\text{vol. of actual}}$

$\left(\frac{1}{4500}\right)^3 = \frac{x}{1800 \times 100 \times 100}$

$\frac{18 \times 100 \times 100 \times 100}{4500 \times 4500 \times 4500} = x$

$= x$

$$\begin{array}{rcl}
 \frac{18}{45 \times 45 \times 45} & = & x \\
 0.00001975 & = & x \\
 \underline{\underline{1.975 \times 10^5 \text{cm}^3}} & = & x
 \end{array}$$

7.

a. $x + 2$ is a factor

$$\begin{array}{rcl}
 x + 2 & = & 0 \\
 x & = & -2 \\
 f(x) & = & 0 \\
 f(-2) & = & 0 \\
 f(x) & = & (3x + 4)^3 - (5x + a)^3 \\
 f(-2) & = & [3(-2) + 4]^3 - [5(-2) + a]^3 \\
 0 & = & (-6 + 4)^3 - (-10 + a)^3 \\
 0 & = & (-2)^3 - (-10 + a)^3 \\
 0 & = & (-2)^3 - (-10 + a)^3 \\
 (-10 + a)^3 & = & (-2)^3 \\
 -10 + a & = & -2 \\
 a & = & -2 + 10 \\
 a & = & \underline{\underline{8}}
 \end{array}$$

b. L.H.S.

$$\begin{aligned}
 &= \frac{\cos^2 A + \tan^2 A - 1}{\sin^2 A} \\
 &= \frac{\cos^2 A + \tan^2 A - 1 (\cos^2 A + \sin^2 A)}{\sin^2 A} \\
 &= \frac{\cos^2 A + \tan^2 A - \cos^2 A - \sin^2 A}{\sin^2 A} \\
 &= \frac{\frac{\sin^2 A}{\cos^2 A} - \sin^2 A}{\sin^2 A} \\
 &= \frac{\sin^2 A}{\sin^2 A - \sin^2 A \cos^2 A} \\
 &= \frac{\sin^2 A \cdot \cos^2 A}{\sin^2 A (1 - \cos^2 A)} \\
 &= \frac{\sin^2 A \cdot \cos^2 A}{\sin^2 A} \\
 &= \frac{\sin^2 A}{\cos^2 A} \\
 &= \tan^2 A \\
 &= \text{R.H.S}
 \end{aligned}$$

L.H.S = R.H.S

Hence proved

$$\begin{aligned}
 \text{c. } \frac{\sqrt{x+1} + \sqrt{x-1}}{\sqrt{x+1} - \sqrt{x-1}} &= \frac{4x-1}{2} \text{ (By C and D)} \\
 \frac{(\sqrt{x+1} + \sqrt{x-1}) + (\sqrt{x+1} - \sqrt{x-1})}{(\sqrt{x+1} + \sqrt{x-1}) - (\sqrt{x+1} - \sqrt{x-1})} &= \frac{4x-1+2}{4x-1-2} \\
 \frac{\sqrt{x+1} + \sqrt{x-1} + \sqrt{x+1} - \sqrt{x-1}}{\sqrt{x+1} + \sqrt{x-1} - \sqrt{x+1} + \sqrt{x-1}} &= \frac{4x+1}{4x-3} \\
 \frac{2\sqrt{x+1}}{2\sqrt{x-1}} &= \frac{4x+1}{4x-3}
 \end{aligned}$$

Squaring both sides,

$$\frac{x+1}{x-1} = \frac{(4x+1)^2}{(4x-3)^2}$$

$$\begin{aligned}
 & \frac{x+1}{x-1} \\
 & \frac{x+1+x-1}{x+1-x+1} \\
 & \frac{2x}{2} \\
 & x \\
 & x(32x-8) \\
 & 32x^2-8x \\
 & 8x \\
 & x \\
 & x \\
 & = \frac{16x^2+8x+1}{16x^2-24x+9} \\
 & = \frac{16x^2+8x+1+16x^2-24x+9}{16x^2+8x+1-16x^2+24x-9} \\
 & = \frac{32x^2-16x+10}{32x-8} \\
 & = \frac{32x^2-16x+10}{32x-8} \\
 & = 32x^2-16x+10 \\
 & = 32x^2-16x+10 \\
 & = 10 \\
 & = \frac{10}{8} \\
 & = 1\frac{1}{4}
 \end{aligned}$$

8.

a. Let the numbers be $a-d$, a , $a+d$

$$a-d+a+a+d = 15$$

$$3a = 15$$

$$a = 5$$

$$\text{G.P: } a-d+1, a+4, a+d+19$$

$$5-d+1, 5+4, 5+d+19$$

$$6-d, 9, 24+d$$

$$\frac{9}{6-d} = \frac{24+d}{9}$$

$$81 = (6-d)(24+d)$$

$$81 = 6(24+d) - d(24+d)$$

$$81 = 144 + 6d - 24d - d^2$$

$$81 = 144 - 18d - d^2$$

$$d^2 + 18d - 63 = 0$$

$$d^2 + 21d - 3d - 63 = 0$$

$$d(d+21) - 3(d+21) = 0$$

$$(d+21)(d-3) = 0$$

$$d+21 = 0 \quad \text{Or} \quad d-3 = 0$$

$$d = -21 \quad \text{Or} \quad d = 3$$

$$a-d+1 = 5-21+1 \quad a-d+1 = 5-3+1$$

$$= -15 \quad = 3$$

$$a+4 = 5+4 \quad a+4 = 5+4$$

$$= 9 \quad = 9$$

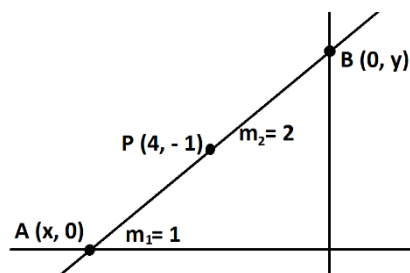
$$a+d+19 = 5-21+19 \quad a+d+19 = 5+3+19$$

$$= 3 \quad = 27$$

$$(3, 9, -15)$$

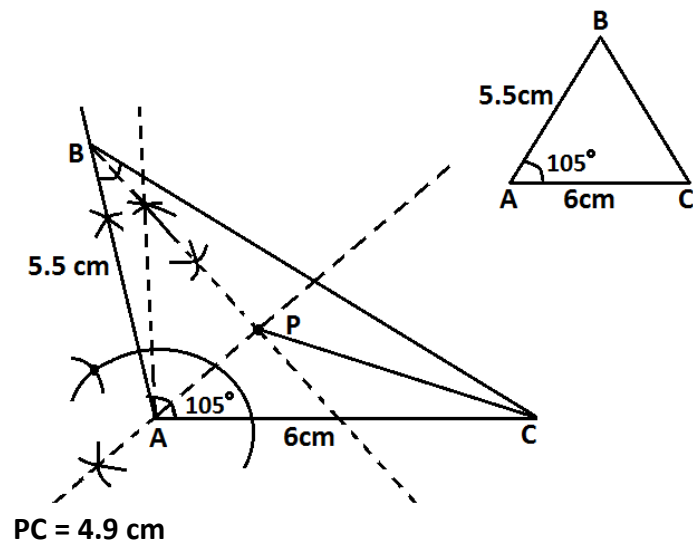
$$(3, 9, 27)$$

b.



$$\begin{aligned}
 \alpha &= \frac{m_1x_2 + m_2x_1}{m_1 + m_2} ; & \beta &= \frac{m_1y_2 + m_2y_1}{m_1 + m_2} \\
 4 &= \frac{(1)(0) + (2)(x)}{1 + 2} ; & -1 &= \frac{(1)(y) + (2)(0)}{1 + 2} \\
 4 &= \frac{0 + 2x}{3} ; & -1 &= \frac{y + 0}{3} \\
 12 &= 2x ; & -3 &= y \\
 x &= 6 ; & y &= -3 \\
 A(x, 0) &= (6, 0) \\
 B(0, y) &= (0, -3)
 \end{aligned}$$

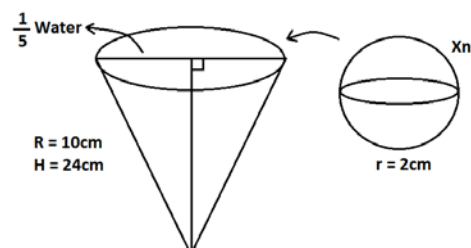
C.



9.

$$\begin{aligned}
 a. \quad a &= \frac{1}{3} \\
 r &= \frac{1}{9} \div \frac{1}{3} \\
 r &= \frac{1}{3} \\
 t_n &= ar^{n-1} \\
 \frac{1}{19683} &= \frac{1}{3} \left(\frac{1}{3} \right)^{n-1} \\
 \frac{1}{19683} &= \left(\frac{1}{3} \right)^{n-1} \\
 \frac{1}{6561} &= \left(\frac{1}{3} \right)^{n-1} \\
 \left(\frac{1}{3} \right)^8 &= \left(\frac{1}{3} \right)^{n-1} \\
 n-1 &= 8 \\
 n &= 9
 \end{aligned}$$

b.



$$\frac{1}{5} (\text{volume of cone}) = n \times \text{volume of sphere}$$

$$\begin{aligned}
 \frac{1}{5} \times \frac{1}{3} \pi R^2 H &= n \times \frac{4}{3} \pi r^3 \\
 \frac{1}{5} \times 10 \times 10 \times 24 &= n \times 4 \times 2 \times 2 \times 2 \\
 n &= \frac{2 \times 10 \times 24}{4 \times 2 \times 2 \times 2} \\
 n &= \underline{\underline{15}}
 \end{aligned}$$

c. In $\triangle ABC$,

$$\tan 60^\circ = \frac{AB}{BC}$$

$$\begin{aligned}
 \sqrt{3} &= \frac{AB}{x} \\
 x\sqrt{3} &= AB \dots\dots (i)
 \end{aligned}$$

In $\triangle ABD$,

$$\tan 30^\circ = \frac{AB}{BD}$$

$$\begin{aligned}
 \frac{1}{\sqrt{3}} &= \frac{AB}{x+60} \\
 \frac{x+60}{\sqrt{3}} &= x\sqrt{3}
 \end{aligned}$$

$$x + 60 = 3x$$

$$3x - x = 60$$

$$2x = 60$$

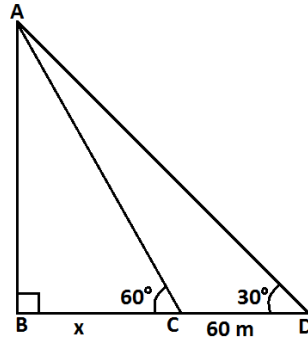
$$x = 30\text{m}$$

$$AB = x\sqrt{3}$$

$$= 30 \times \frac{1732}{1000}$$

$$= 51.96\text{ m}$$

$$= \underline{\underline{52\text{ m}}}$$



10.

$$a. \frac{4}{3} \pi r^3 = \pi h (r_1^2 - r_2^2)$$

$$\frac{4}{3} \times 6 \times 6 \times 6 = 72 (4^2 - r_2^2)$$

$$16 - r_2^2 = 4$$

$$r_2^2 = 16 - 4$$

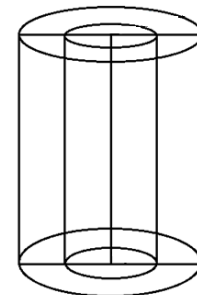
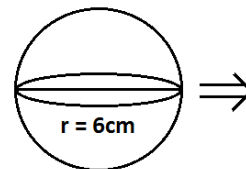
$$r_2^2 = 12$$

$$r_2 = \sqrt{12}$$

$$r_2 = \underline{\underline{3.46\text{cm}}}$$

$$\begin{aligned}
 \text{thickness} &= r_1 - r_2 \\
 &= 4 - 3.46
 \end{aligned}$$

$$= \underline{\underline{0.54\text{cm}}}$$



$$r_1 = 4\text{cm}$$

$$r_2 = ?$$

$$h = 72\text{cm}$$

b.

CI	F	cf
0 – 10	16	16
10 – 20	9	25
20 – 30	5	30
30 – 40	18	48
40 – 50	22	70
50 – 60	26	96
60 – 70	3	99
70 – 80	4	103
80 – 90	6	109

90 – 100	11	120
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$$\begin{aligned} \text{i. Me} &= \frac{n^{\text{th}}}{2} \text{ term} \\ &= 60^{\text{th}} \text{ term} \\ &= 47 \end{aligned}$$

$$\begin{aligned} \text{ii. } Q_1 &= \frac{n^{\text{th}}}{4} \text{ term} \\ &= 30^{\text{th}} \text{ term} \\ &= 30 \end{aligned}$$

$$\begin{aligned} Q_3 &= \frac{3n^{\text{th}}}{4} \text{ term} \\ &= 90^{\text{th}} \text{ term} \\ &= 58 \end{aligned}$$

$$\begin{aligned} \text{Interquartile} &= Q_3 - Q_1 \\ &= 58 - 30 \\ &= 28 \end{aligned}$$

iii. 17

11.

$$\begin{aligned} \text{a. L.H.S} &= \frac{\cot^2 A}{(\operatorname{cosec} A + 1)^2} \\ &= \frac{\operatorname{cosec}^2 A - 1}{(\operatorname{cosec} A + 1)^2} \{ \operatorname{cosec}^2 A - 1 = \cot^2 A \} \\ &= \frac{(\operatorname{cosec} A - 1)(\operatorname{cosec} A + 1)}{(\operatorname{cosec} A + 1)(\operatorname{cosec} A + 1)} \\ &= \frac{\operatorname{cosec} A - 1}{\operatorname{cosec} A + 1} \\ &= \left(\frac{1}{\sin A} - 1 \right) \div \left(\frac{1}{\sin A} + 1 \right) \\ &= \frac{1 - \sin A}{1 + \sin A} \times \frac{\sin A}{1 + \sin A} \\ &= \frac{\sin A}{1 + \sin A} \\ &= \text{R.H.S} \end{aligned}$$

$$\text{L.H.S} = \text{R.H.S}$$

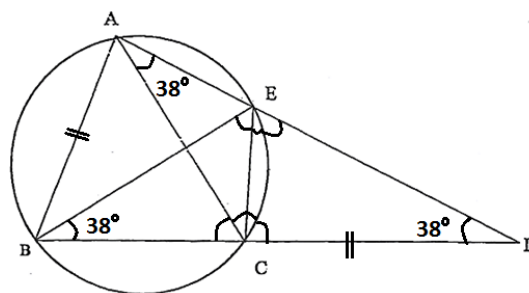
Hence proved

b. Given:

- i. $AB = AC = CD$
- ii. $\angle ADC = 38^\circ$

To find:

- i. $\angle ABC$
- ii. $\angle BEC$



	Statement	Reason
1.	In $\triangle ACD$,	
i.	$AC = CD$	Given
ii.	$\angle ADC = \angle DAC = 38^\circ$	Angles opposite equal sides are equal
iii.	$\angle ADC + \angle DAC + \angle ACD = 180^\circ$	Sum of all angles of a triangle is 180°
	$38^\circ + 38^\circ + \angle ACD = 180^\circ$	
	$76^\circ + \angle ACD = 180^\circ$	
	$\angle ACD = 104^\circ$	
2.	$\angle ACB + \angle ACD = 180^\circ$	Linear pair
	$\angle ACB + 104^\circ = 180^\circ$	

3.	$\angle ACB = 76^\circ$ In $\triangle ABC$,	
i.	$AB = AC$	Given
ii.	$\angle ABC = \angle ACB = 76^\circ$ $\angle ABC = 76^\circ$	Angles opposite equal sides are equal.
iii.	$\angle ABC + \angle ACB + \angle BAC = 180^\circ$ $76^\circ + 76^\circ + \angle BAC = 180^\circ$ $152^\circ + \angle BAC = 180^\circ$ $\angle BAC = 28^\circ$	Sum of all angles of triangle 180°
4.	$\angle BAC = \angle BEC = 28^\circ$	Angles in the same segment are equal.

C.

$$\begin{aligned}
 \text{i. } 4y &= 3x + 8 \\
 4y &= 3(0) + 8 \\
 4y &= 0 + 8 \\
 y &= 2 \\
 \therefore A &= (0, 2) \\
 \text{ii. } 4y &= 3x + 8 \\
 y &= \frac{3x}{4} + \frac{8}{4} \\
 m &= \frac{3}{4} \\
 \therefore m \text{ of AB} &= \frac{-1}{m \text{ of AC}} \text{ (perpendicular lines)} \\
 \therefore \text{The equation is,} \\
 m &= \frac{y - y_1}{x - x_1} \\
 \frac{-4}{3} &= \frac{y - 2}{x - 0} \\
 -4(x - 0) &= (y - 2) 3 \\
 -4x + 0 &= 3y - 6 \\
 0 &= 4x + 3y - 6 \\
 \text{iii. } 3y + 4x - 6 &= 0 \\
 3(0) + 4x - 6 &= 0 \\
 4x &= 6 \\
 x &= \frac{3}{2} \\
 \therefore B &= \left(\frac{3}{2}, 0\right)
 \end{aligned}$$

Answers been written by students may have caused spelling errors.